



*A mechanistic approach to predict  
the probability of complication  
in the rat spinal cord  
following particle irradiation*



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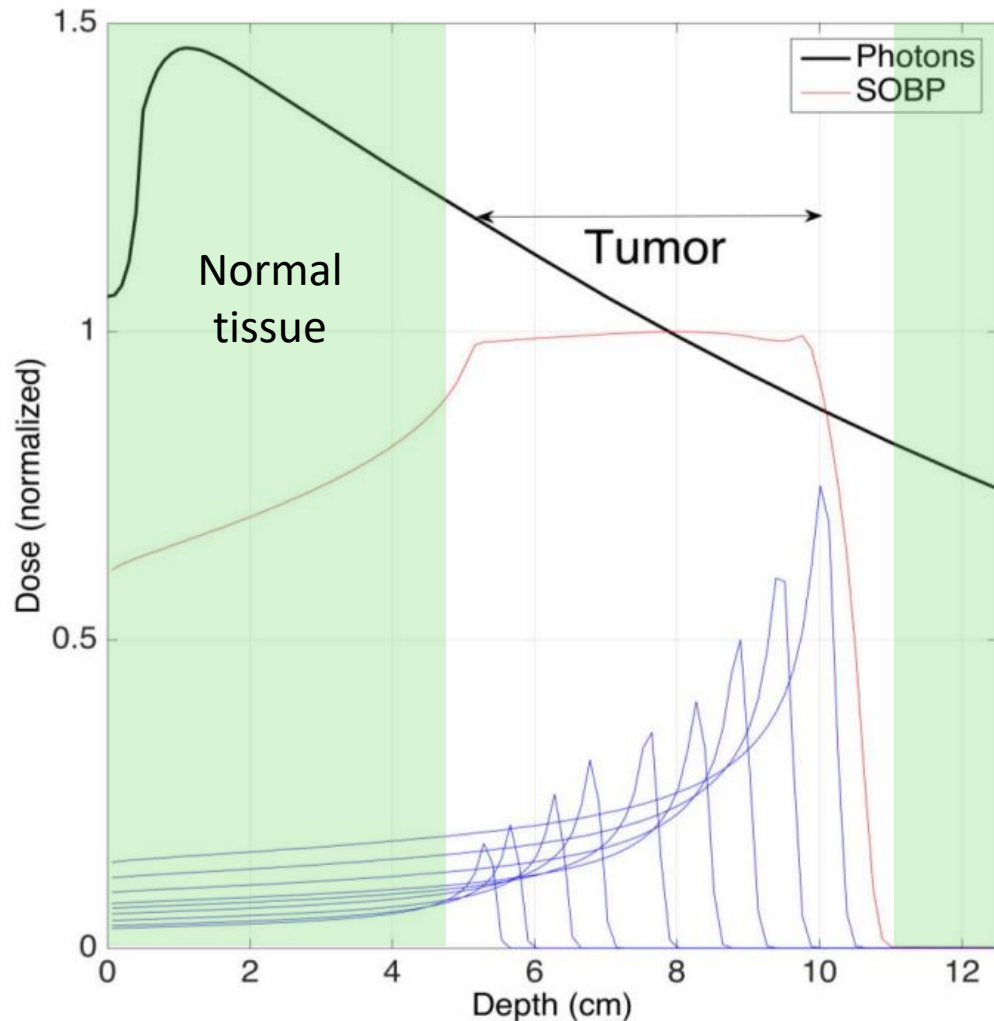
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# *Introduction*

# Hadrontherapy

This study was conducted within the framework of **innovative radiotherapy** techniques, among which Hadrontherapy stands out.



[Image credit: E. Sterpin, Université catholique de Louvain]

*Hadrontherapy* =  
**charged particle irradiation**

- ↓
- ✓ **High radiation doses to tumour cells** enabled by the Spread-Out Bragg Peak (**SOBP**) produced by charged particles
  - ✓ **Spare surrounding healthy tissues**, compared to conventional photon radiotherapy

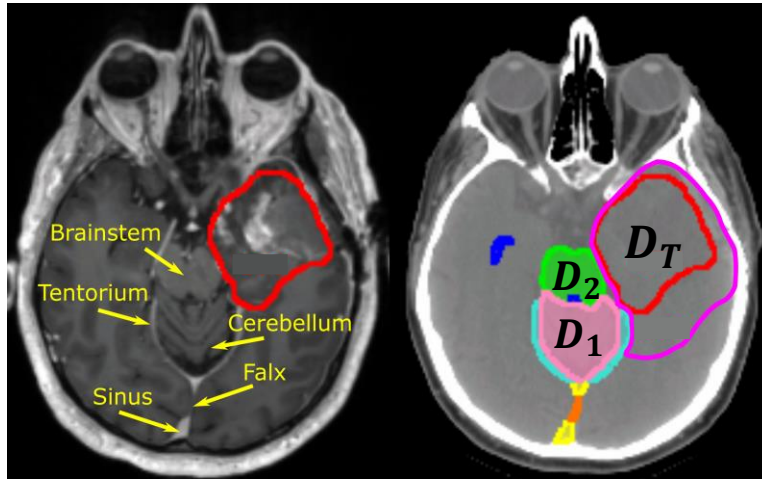
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Well-suited for :

- pediatric tumours
- tumours located near organs at risk

# Treatment planning in Hadrontherapy

TODAY



[Image credit: The Cancer Imaging Archive]

$D_T$  = Tumour dose > 50 Gy

$D_1$  = OAR 1 < 2 Gy

$D_2$  = OAR 2 < 3 Gy

- Prescribed **reference dose** ( $D_T$ ) to the **tumor** site
- Respecting certain **dose limits** in nearby **organs at risk** (e.g.  $D_1$ ,  $D_2$ )

TOMORROW

To develop treatment plans directly based on the *clinical outcomes*



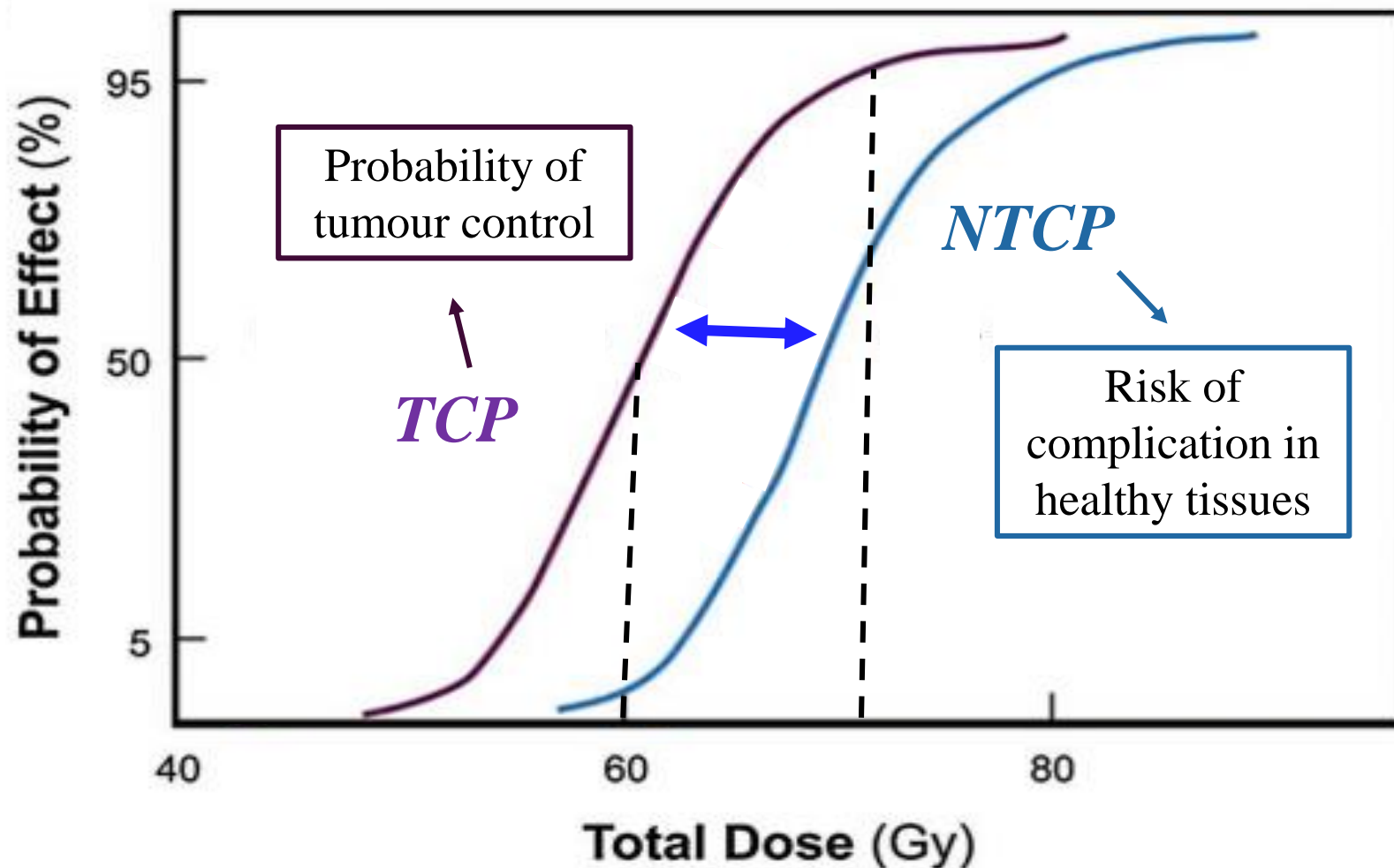
**Aim:**

- optimize therapeutic efficacy
- minimize side effects
- develop more *patient-specific* treatment plans

To quantify the clinical *outcomes*



*Tumour Control Probability (TCP)*  
*Normal Tissue Complication Probability (NTCP)*  
*curves*



**Hadrontherapy Aim:**

- maximize *TCP*
- minimize *NTCP*

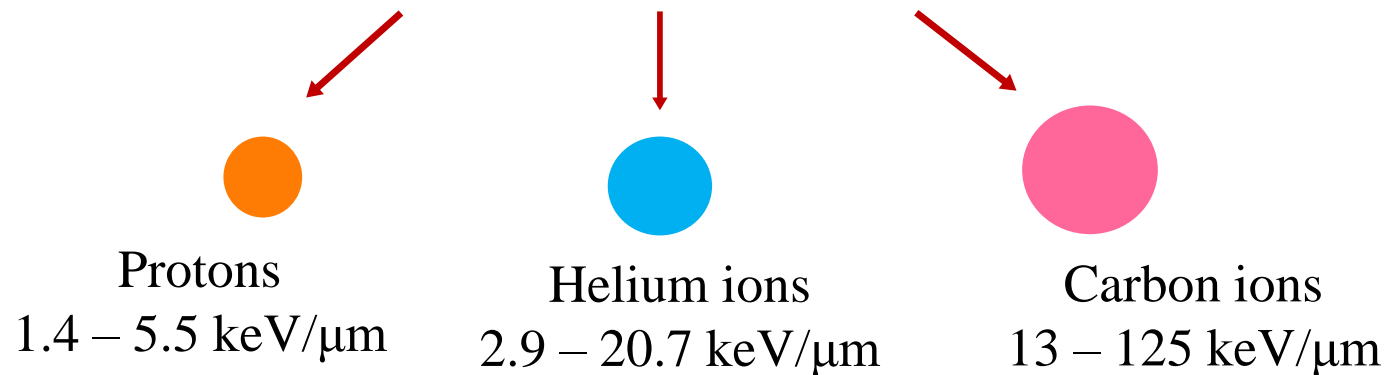


increase *TCP* – *NTCP*  
gap as much as possible

# *AIM of the study*

Development of a **novel approach** to **predict NTCP** curves for **late tissue reactions** following **Hadrontherapy**

For **rat spinal cord** irradiated with:



In case of:

Monochromatic  
irradiation

Real mixed  
field

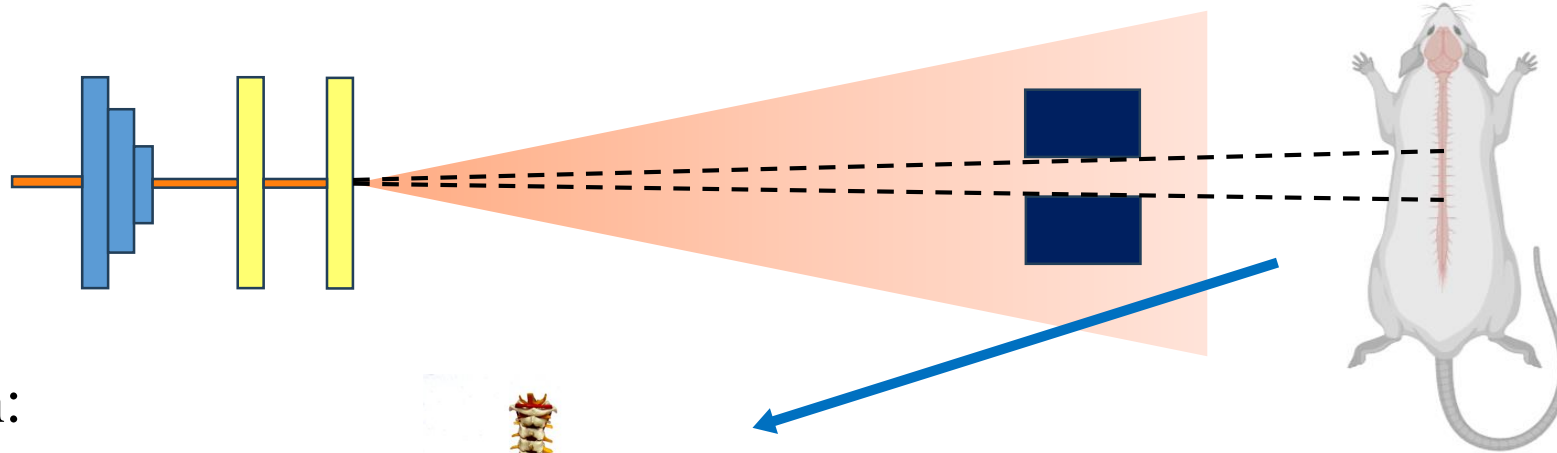


To directly incorporate **biological outcomes** into hadrontherapy treatment planning to improve **personalization** and clinical effectiveness

*Materials  
and  
Methods*

# Experimental Data

The experimental data, obtained from the literature, were used both for **parameter calibration** and for the **validation** of ion NTCP predictions. Further details can be found in [Karger et al., Int. J. Radiat. Onc. Biol. Phys., 2006, [10.1016/j.ijrobp.2006.08.045](https://doi.org/10.1016/j.ijrobp.2006.08.045)].



Irradiation with:

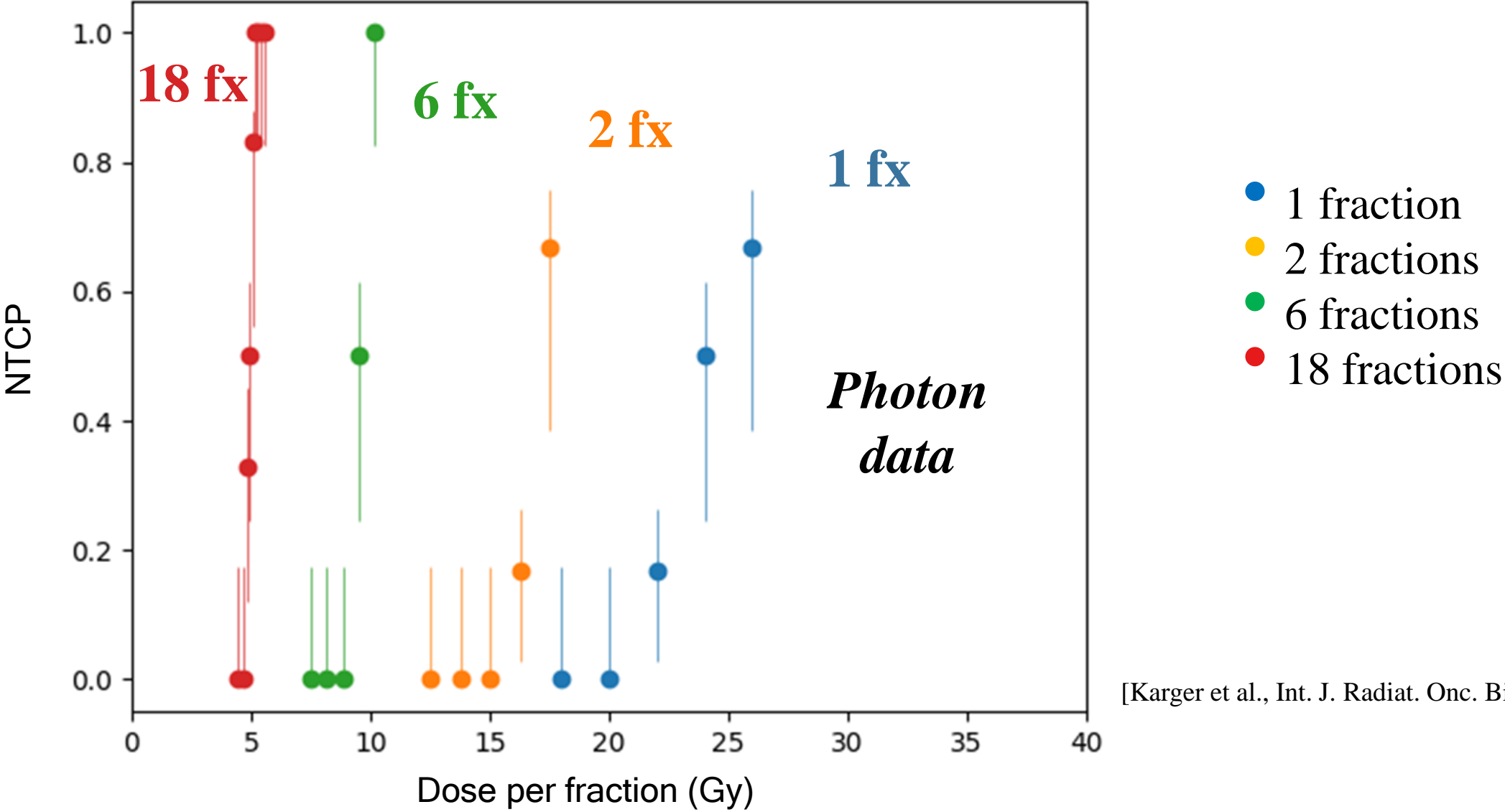
- Photons (for **parameter calibration**)
  - Protons
  - Helium ions
  - Carbon ions
- for **ion NTCP validation**



A portion of the rat spinal cord was irradiated

*Clinical outcome:*  
**paresis of grade II**,  
which is a late tissue  
reaction

# *e. g. Experimental Data*



[Karger et al., Int. J. Radiat. Onc. Biol. Phys., 2006]

# Critical Element NTCP Model

[Withers et al., Int. J. Radiat. Onc. Biol. Phys., 1988]

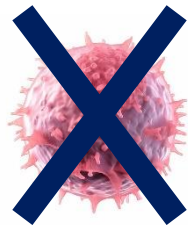
We selected the **Critical Element NTCP model**, which is based on the concept of Functional Sub-Units (FSUs).

*Functional Sub-Unit (FSU)*



**Basic unit** that can  
maintain organ functionality

*Probability of  
killing 1 cell*

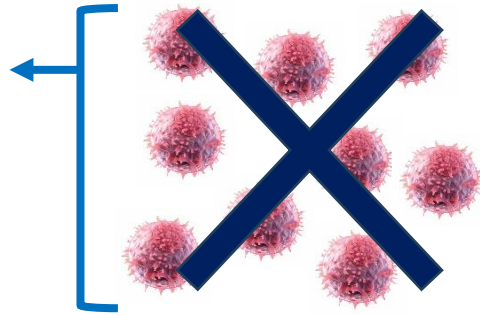


Linear-Quadratic cell  
survival model (LQ)

$$P_{cell} = 1 - \textcircled{S} = 1 - e^{-\alpha nd - \beta nd^2}$$

**Assumption:**

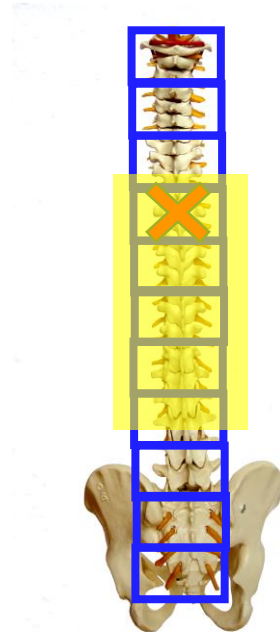
1 FSU  
=  
k cells



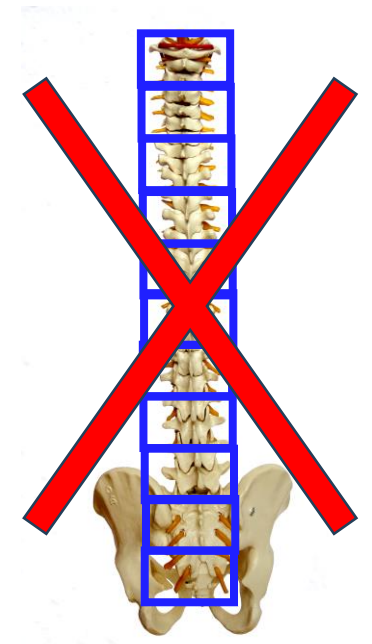
Probability of depleting 1 FSU =  
probability of killing all its k cells

$$P_{FSU} = (1 - e^{-\alpha nd - \beta nd^2})^k$$

For **serial organs**, like  
the spinal cord, the **loss**  
of a **single FSU** is  
sufficient to lack the  
functionality of the **entire**  
**organ**



*N*: # tot  
irradiated  
FSUs



$$\text{NTCP} = 1 - (1 - P_{FSU})^N = 1 - \left[ 1 - (1 - e^{-\alpha nd - \beta nd^2})^k \right]^N$$

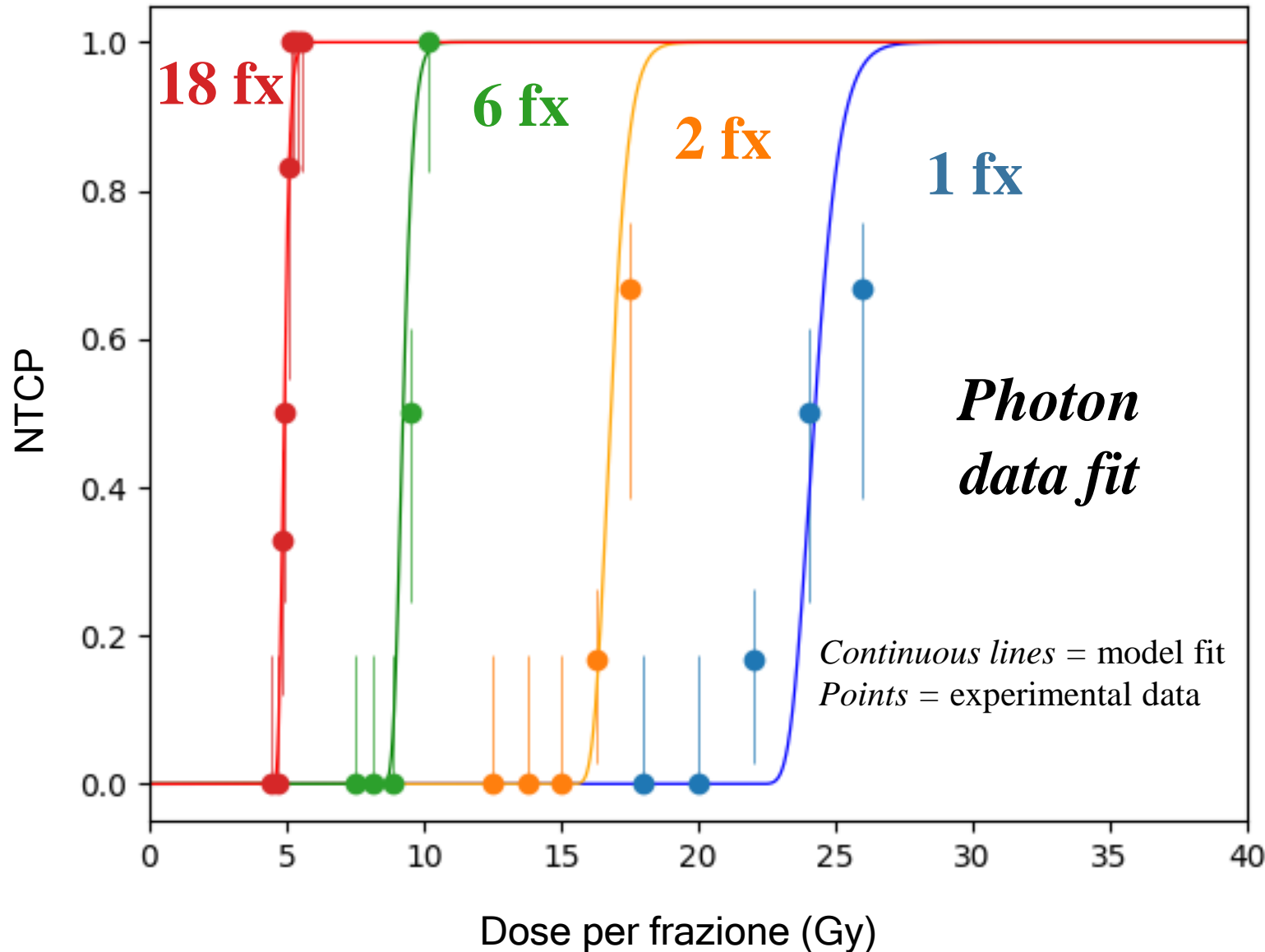
NTCP model that depends on **only 4 parameters**



**Model parameter estimation for ion NTCP predictions:**

One set of ion  **$\alpha$ ,  $\beta$ ,  $k$ ,  $N$**  parameters for all the fractionation schemes

# *k and N estimation for ion NTCP predictions*



**Photon data fitted** with the *Critical Element NTCP Model*

Resulting parameters

Photon **k, N**  
depending only  
on tissue features

Photon  
 $\alpha_X$  and  $\beta_X$

**Fixed** for ion  
NTCP predictions

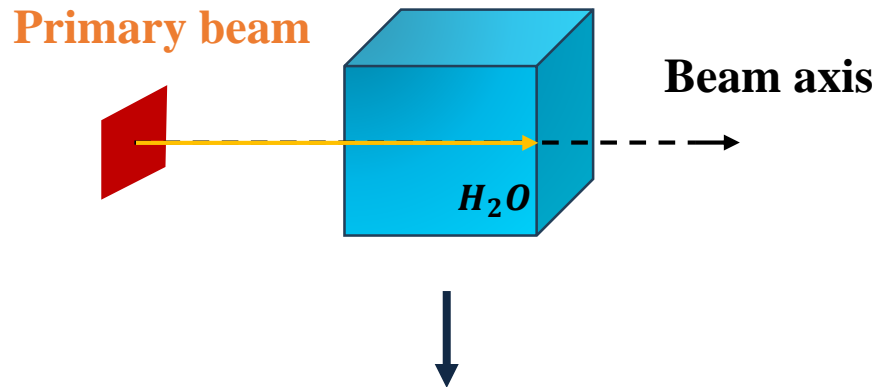
# Ion $\alpha$ and $\beta$ estimation for ion NTCP predictions

In case of

①

**Monochromatic irradiation**

- Only **primary beam** particles at **fixed energy** were considered

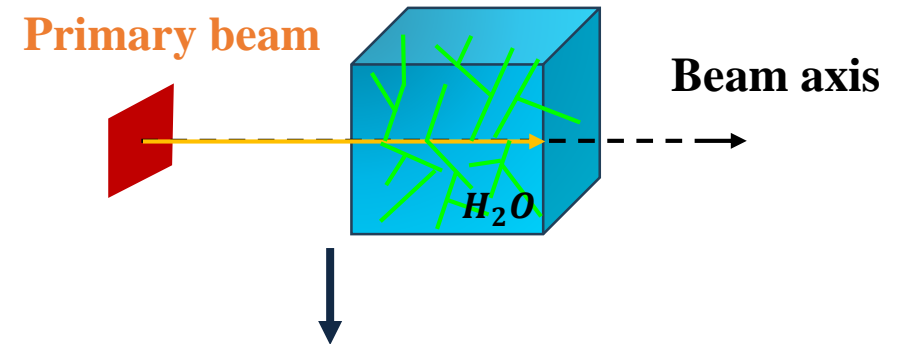


**BIANCA**

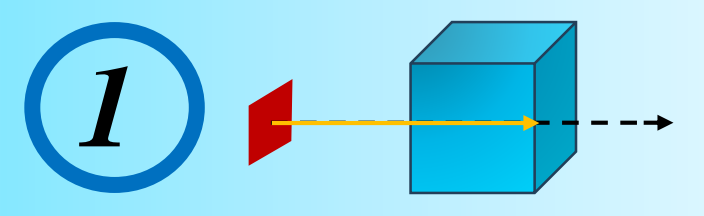
②

**Real Mixed Field**

- All **secondary particles** produced by the interaction of the primary beam with the water phantom were included
- The SOBP results from the superposition of Bragg peaks at **different energies**



**Interface BIANCA - GEANT4**



# Monochromatic Field

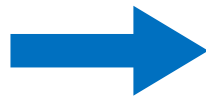


Ion  $\alpha$  and  $\beta$   $\rightarrow$  calculated by applying **BIANCA** model

**BIANCA:** biophysical model developed by the Computational Radiobiology group of Pavia University [Ballarini, Carante, Radiat. Phys. And Chem., 2016]

BIANCA input

Photon  $\alpha_X$  and  $\beta_X$  derived by fitting the photon data using the Critical Element NTCP model



```

Z=1 A=1,2,3
LET   alfa      beta
5      0.161168003608071 0.034227925863557
7.5    0.219155512347106 0.031807059167825
10     0.277730304065006 0.026062986984213
12.5   0.324223249128924 0.031963531745716
15     0.370061833526514 0.032195025167274
17.5   0.421451839190716 0.031121716722449
20     0.482515824349661 0.028525693688078
22.5   0.560520033338037 0.018863044675061
25     0.613244623202487 0.019486893814967
27.5   0.670278414247874 0.018719108913174
30     0.723636950773347 0.019048357687813

Z=2 A=3 (He3)
LET   alfa      beta
5      0.134484868252636 0.033328267759041
10     0.144914045351193 0.039167916406686
20     0.195309536204132 0.055766427339300
30     0.254263496879065 0.086614721872234
40     0.346232798363745 0.110820821623133
50     0.461751927355611 0.125899692117198
60     0.577156328111620 0.149414730517834
70     0.688177599469057 0.170307321062664
80     0.831202131850177 0.173711239896555
90     0.958976414546513 0.178987749762615

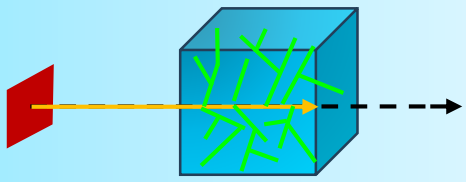
Z=2 A=4 (He4)
LET   alfa      beta
5      0.122919965474113 0.0282243396663055
10     0.164742642147497 0.0320256389518587

```

BIANCA output

Dataset of  $\alpha$  and  $\beta$  for each **particle** and **LET** value

2



## *Real Mixed Field*

Ion  $\alpha$  and  $\beta$   $\rightarrow$  calculated by **BIANCA – GEANT4** interface

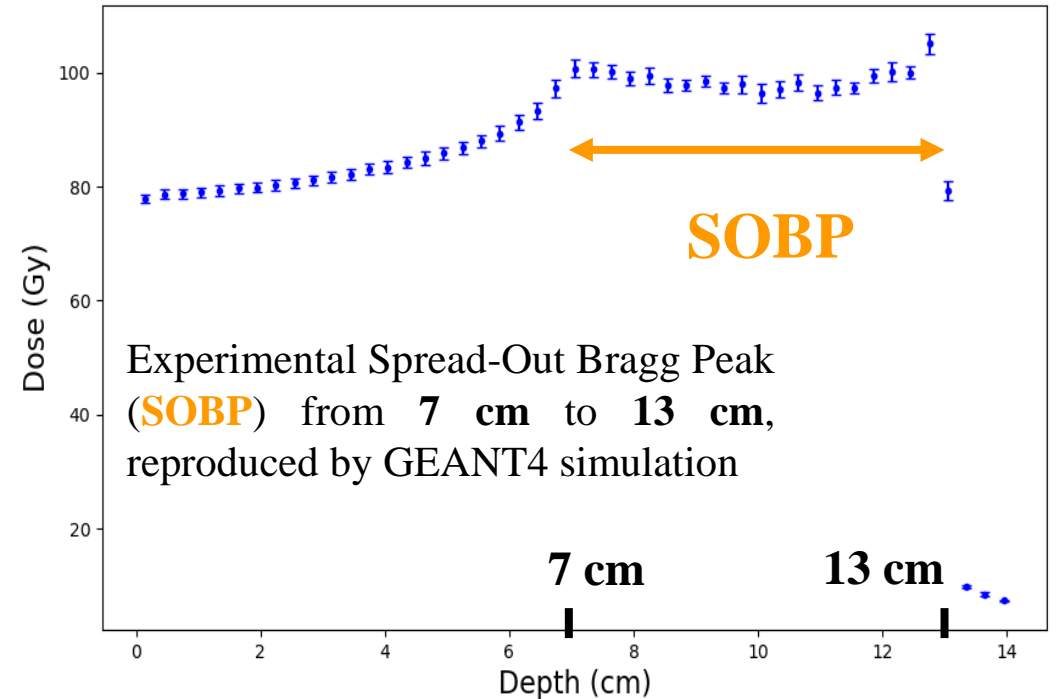
### GEANT4 irradiation simulation:

To reproduce the **experimental conditions** and identify the secondary particles generated

**BIANCA**  $\alpha$  and  $\beta$  table for each particle, as a function of energy value



The ion  $\bar{\alpha}$  and  $\bar{\beta}$  values for the mixed field were calculated by **averaging, over dose**, the  $\alpha$  and  $\beta$  values read from the BIANCA table **for each energy and particle type** produced in the GEANT4 simulation



# *Ion NTCP predictions*

➤ All four parameters required for ion NTCP predictions have been estimated



$\alpha, \beta$  Monochromatic Field  
from BIANCA



$k, N$   
from Photon data fit



$\bar{\alpha}, \bar{\beta}$  Real Mixed Field  
from BIANCA-GEANT4

➤ Monochromatic Field

$$\text{NTCP} = 1 - \left[ 1 - \left( 1 - e^{-\alpha nd - \beta nd^2} \right)^k \right]^N$$

➤ Real Mixed Field

$$\text{NTCP} = 1 - \left[ 1 - \left( 1 - e^{-\bar{\alpha} nd - \bar{\beta} nd^2} \right)^k \right]^N$$

NO free - parameters



Full **predictions** of  
ion NTCP curves

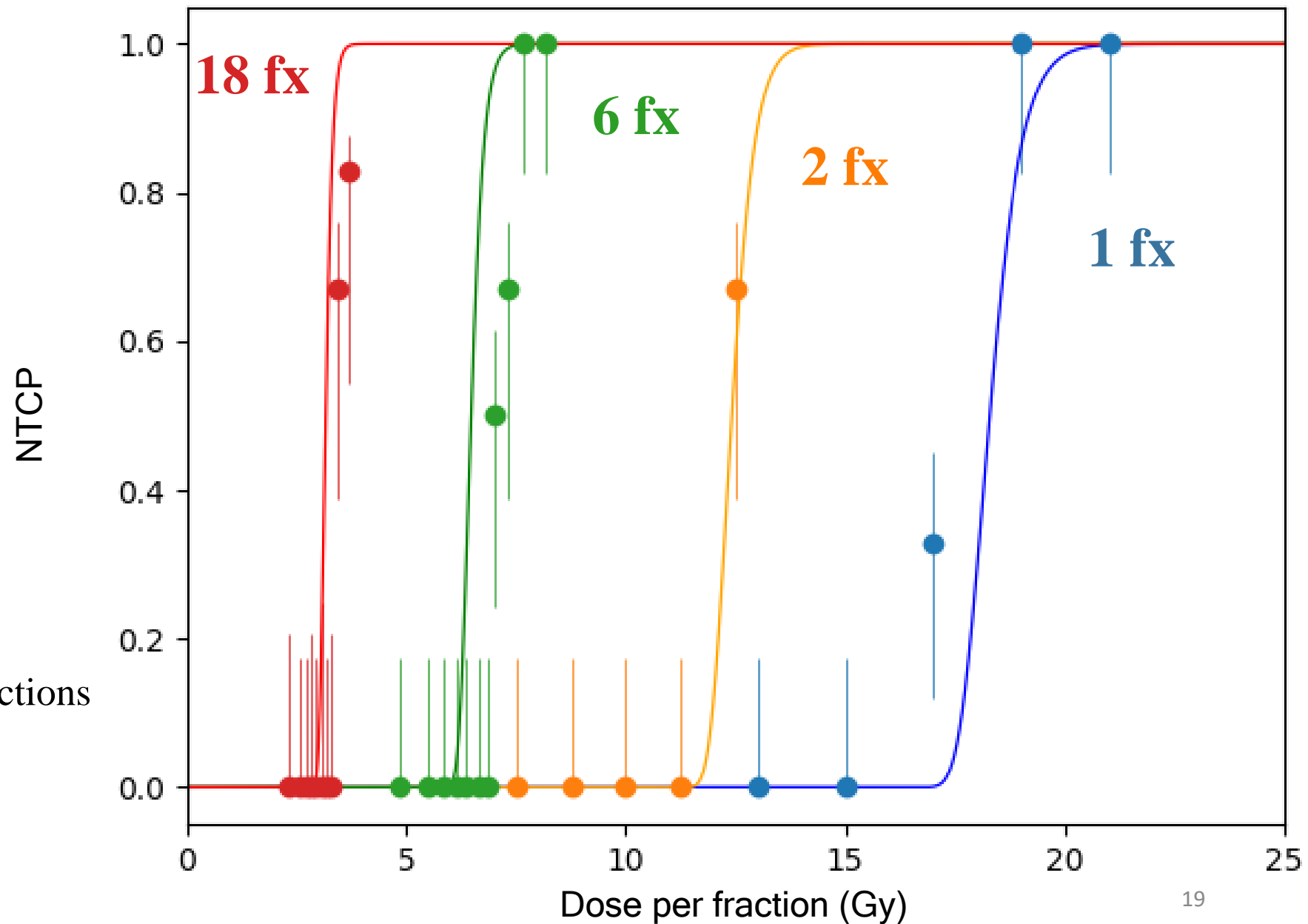
# *Results*

# Carbon ions 13 keV/ $\mu\text{m}$

**Monochromatic  
Field**

- 1 fraction
- 2 fractions
- 6 fractions
- 18 fractions

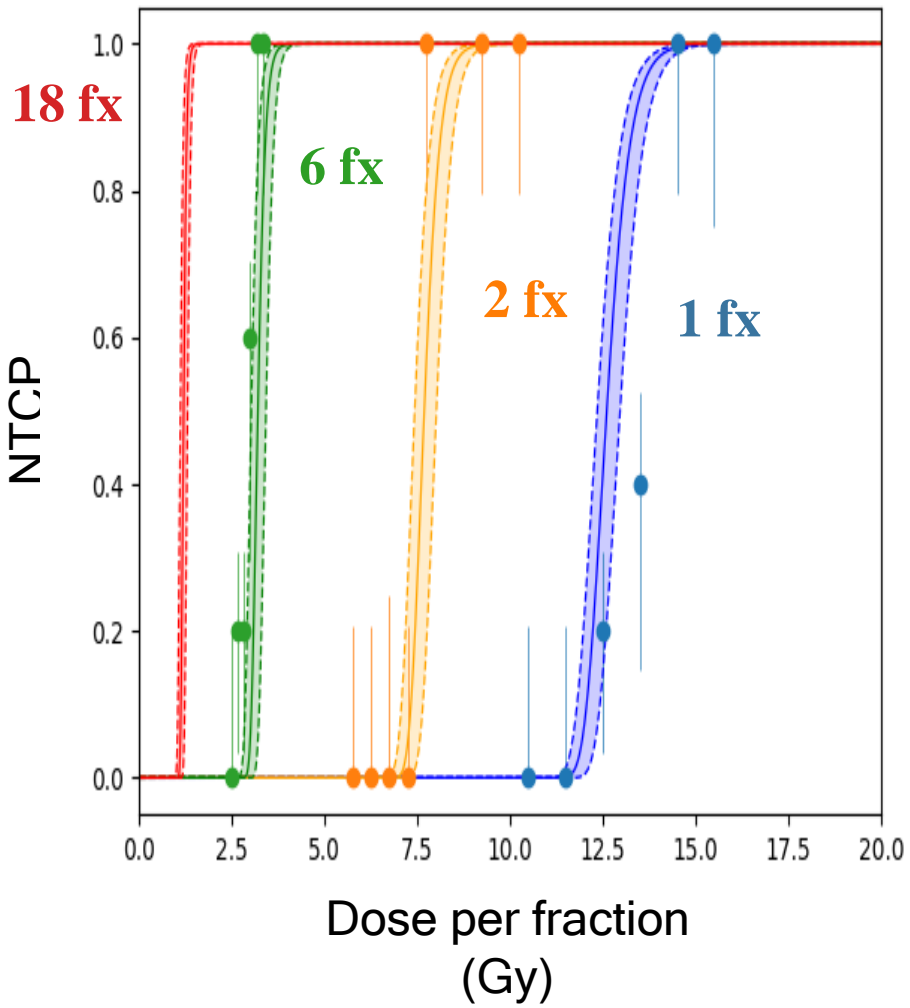
*Continuous lines:* model predictions  
*Points:* experimental data



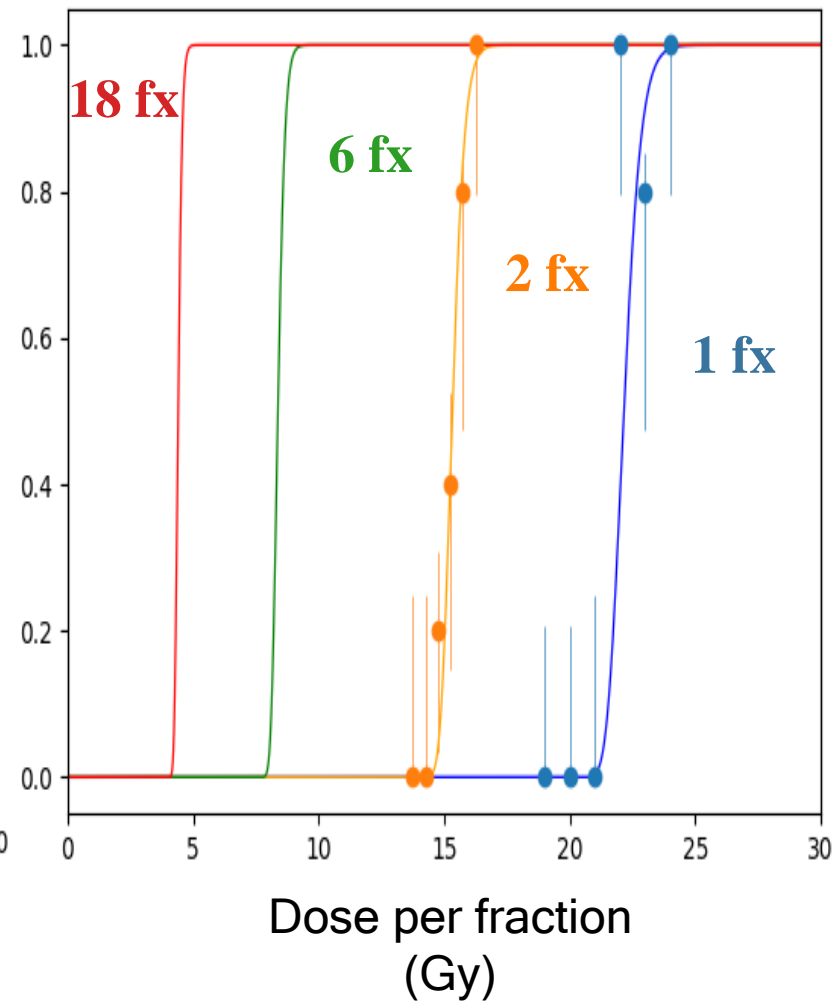
# Monochromatic Field

Results for other particles and LET values

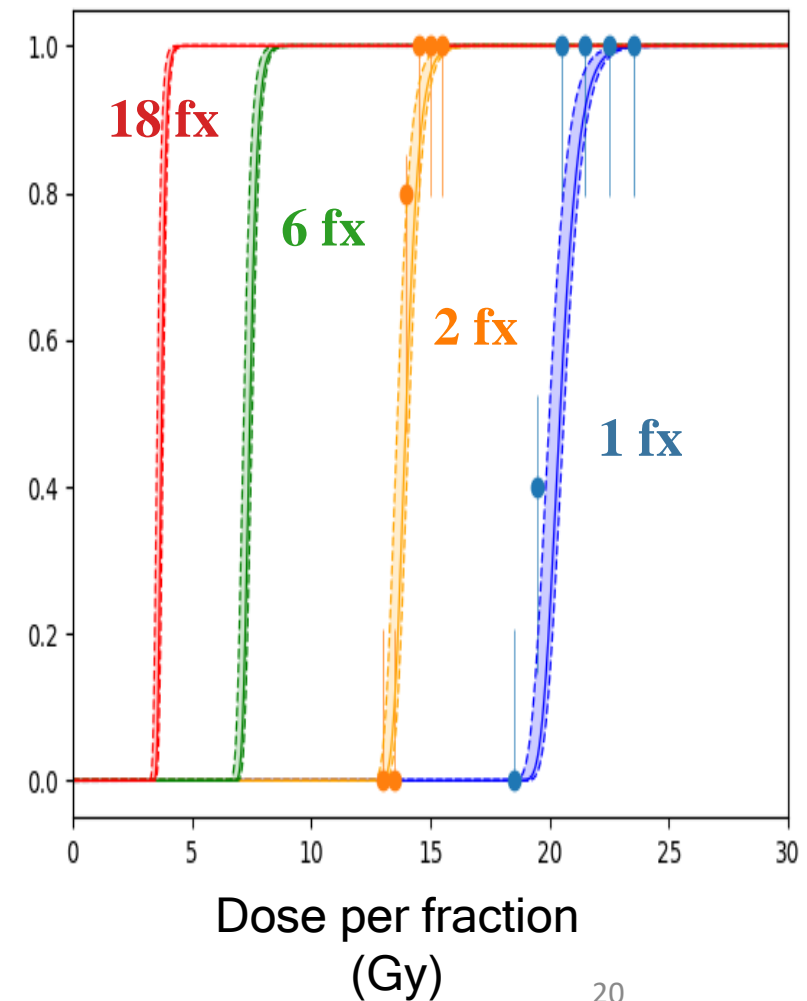
*Carbon ions  $99 \pm 13 \text{ keV}/\mu\text{m}$*

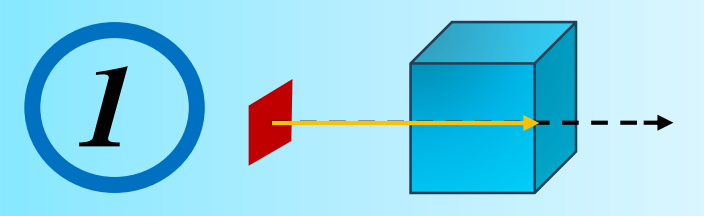


*Helium ions  $2.9 \text{ keV}/\mu\text{m}$*



*Protons  $5.5^{+1.6}_{-0.6}$*

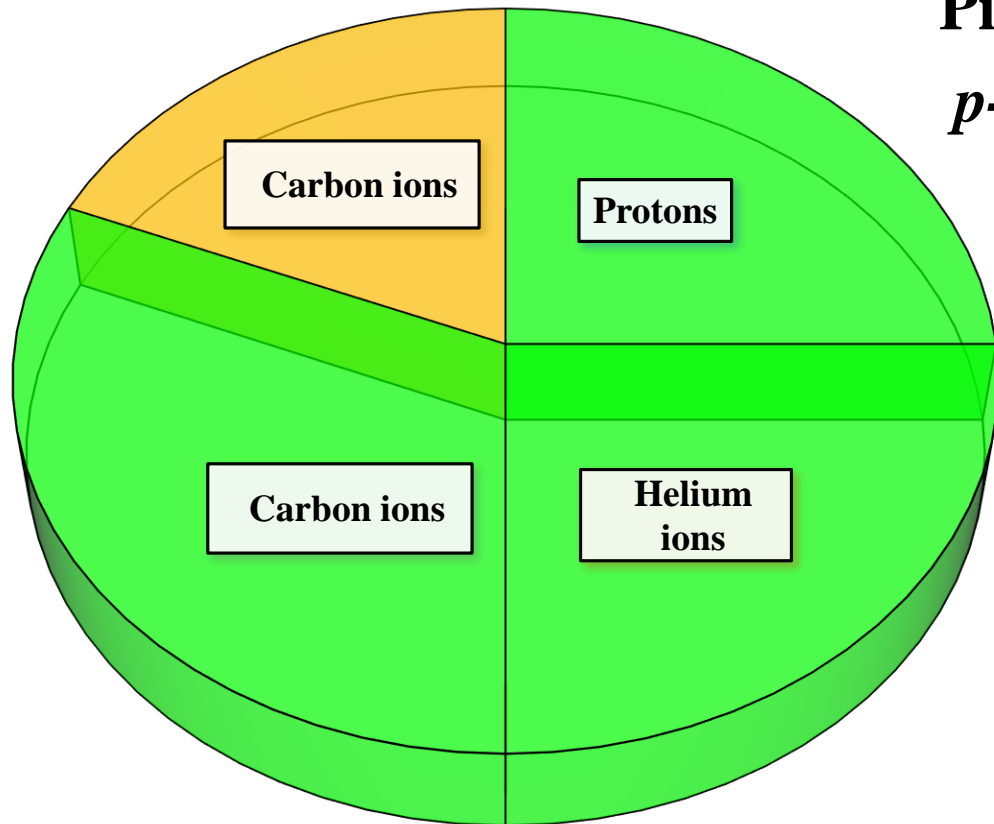




# Statistical analysis

Monochromatic  
Field

*P-values* assessing the agreement between experimental data and our approach predictions under monochromatic ion irradiation were obtained via **Monte Carlo simulation**.



Pie chart of  
*p-values*

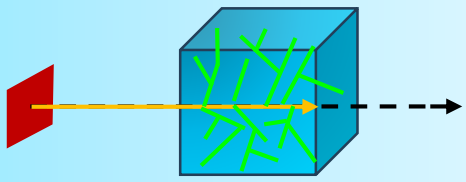
$p - value > 5\%$



$p - value > 1\%$

OK

In general, the proposed approach exhibits **good predictive power** across the entire set of experimental data.



Regarding real mixed-field ion irradiation, only the **percentage difference** between the monochromatic and mixed-field cases was evaluated.

Percentage difference

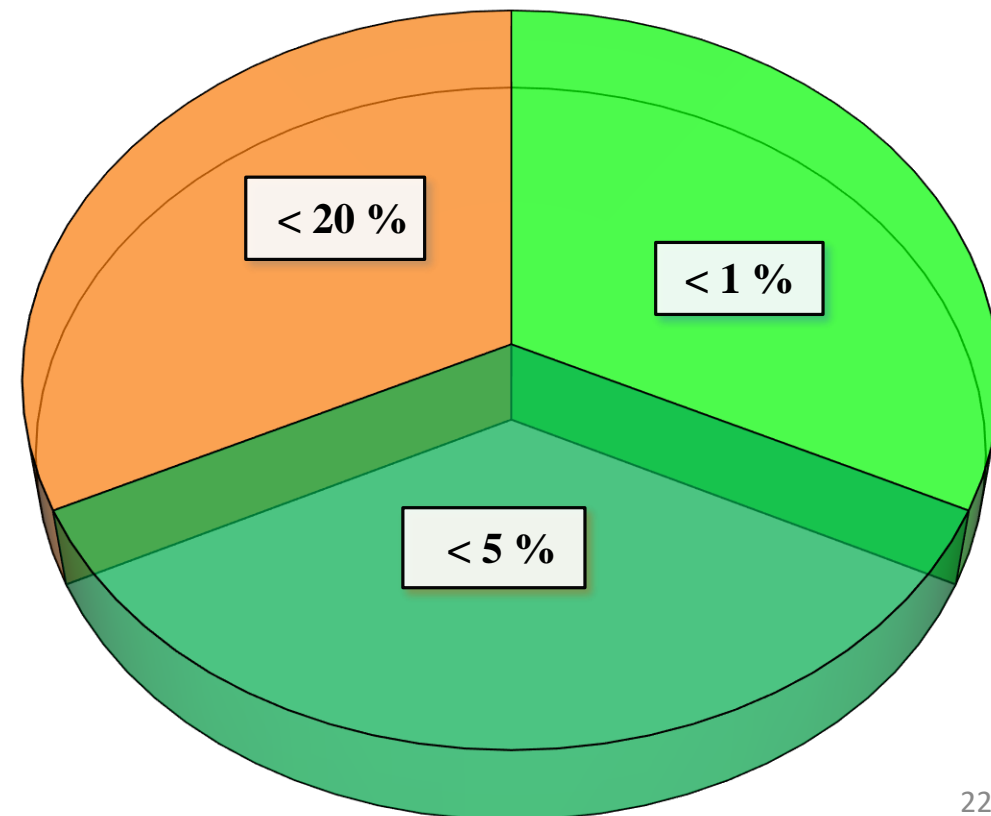
$$= \frac{|D_{50}^{mixed} - D_{50}^{mono}|}{D_{50}^{mono}} \cdot 100$$

$D_{50}^{mixed}$  : dose at a NTCP of 50% in case of real mixed field

$D_{50}^{mono}$  : dose at a NTCP of 50% in case of monochromatic field

Out of 56 datasets, 47 show **NO significant difference** (< 5%) between the two scenarios. Differences > 5% but < 20% were observed only in few C-ions cases with high LET, where mixed-field plays an important role.

Pie chart of percentage difference mixed-mono



# *Conclusions*

# Take home messages

Integration of  
**biological models**  
**(TCP / NTCP)**  
into *treatment planning*



To enable  
*patient-specific*  
treatment plans

Strengths of  
**our approach**

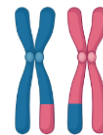
[A. Casali et al., Phys. Med. Biol., 2024]



- $NTCP(k, N, \alpha, \beta)$**
- ✓ few parameters
  - ✓ high predictive power

Advantage of using  
**BIANCA** over other  
biophysical models

BIANCA simulates also  
**chromosome aberrations**



To predict  
**stochastic effects**



# *Future perspectives*

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➤ Apply NTCP *Critical Element Model* + LQ model + BIANCA to



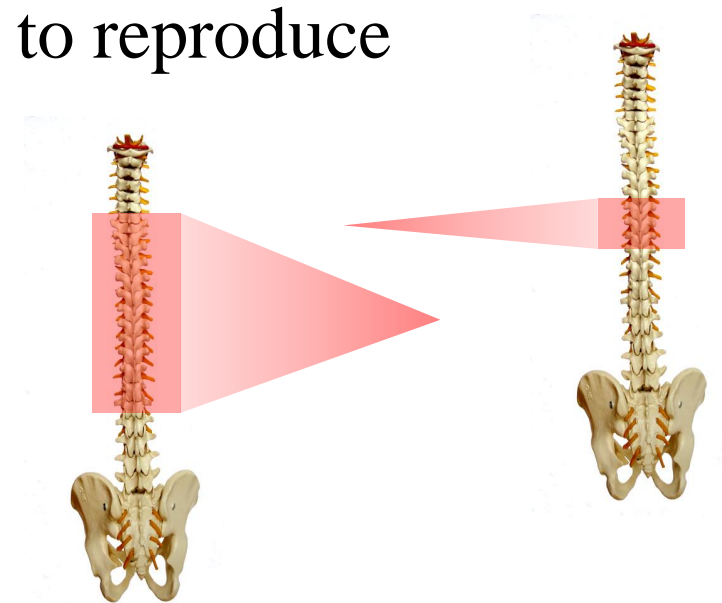
- **Human data**
- Other *tissue reactions* endpoints
- Other *irradiated organs*

➤ Modify the NTCP model **mathematical expression** to reproduce



- **Stochastic effects**  
(es. radiation-induced tumours)

- **Volume Effect**



***Thank you for your  
attention!***

If you have any doubts, questions, or if you want more information, please don't hesitate to contact me



**alice.casali01@universitadipavia.it**